Name: $\qquad$ No. $\qquad$ Per: $\qquad$ Date: $\qquad$

Proofs Practice - "Proofs Worksheet \#2"
$2 C$


1. Given: $O$ is the midpoint of $\mathrm{MN} \quad$ Prove: $\mathrm{OW}=\mathrm{ON}$ $O M=O W$

|  | Statement | Reason |
| :--- | :--- | :--- |
| 1. | O is the midpoint of seg MN | Given |
| 2. | Segment NO = Segment OM | Def of midpoint |
| 3. | NO = OM | Def of cong. |
| 4. | OM = OW | Given |
| 5. | NO = OW | Transitive Property (Substitution) |
|  |  |  |
| 6. | OW - NO | Symmetric Property |
| 7. | NO = ON | Reflexive Property |
| 8. | OW = ON | Transitive Property (Substitution) |


2. Given: $A B=C D$

Prove: $A C=B D$

|  | Statement | Reason |
| :--- | :--- | :--- |
| 1. | $A B=C D$ | Given |
| 2. | $A B+B C=C D+B C$ | Addition Property of Equality |
| 3. | $A B+B C=A C$ | Segment Addition Post |
| 4. | $C D+B C=B D$ | Segment Addition Post |
| 5. | $A C=B D$ | Substitution |


3. Given: $\mathrm{m} \angle 1=90^{\circ}$

Prove: $m \angle 2=90^{\circ}$

|  | Statement | Reason |
| :--- | :--- | :--- |
| 1. | $\mathrm{m} \angle 1=90^{\circ}$ | Given |
| 2. | $\angle 1$ and $\angle 2$ are a linear pair | Definition of Linear Pair |
| 3. | $\angle 1$ and $\angle 2$ are supplementary | Linear Pair Theorem |
| 4. | $\mathrm{m} \angle 1+\mathrm{m} \angle 2=180^{\circ}$ | Definition of Supplementary |
| 5. | $90^{\circ}+\mathrm{m} \angle 2=180^{\circ}$ | Substitution |
| 6. | $\mathrm{~m} \angle 2=90^{\circ}$ | Subtraction Prop of Equality |


4. Given: $\angle 1$ and $\angle 2$ are complementary Prove: $\mathrm{m} \angle 1=\mathrm{m} \angle 3$
$\angle 3$ and $\angle 2$ are complementary

|  | Statement | Reason |
| :---: | :--- | :--- |
| 1. | $\angle 1$ and $\angle 2$ are complementary <br> $\angle 3$ and $\angle 2$ are complementary | Given |
| 2. | $\mathrm{m} \angle 1+\mathrm{m} \angle 2=90^{\circ}$ <br> $\mathrm{m} \angle 3+\mathrm{m} \angle 2=90^{\circ}$ | Definition of Complementary |
| 3. | $\mathrm{m} \angle 1+\mathrm{m} \angle 2=\mathrm{m} \angle 3+\mathrm{m} \angle 2$ | Substitution |
| 4. | $\mathrm{m} \angle 1=\mathrm{m} \angle 3$ | Subtraction Prop of Equality |


5. Given: $\mathrm{m} \angle 1=\mathrm{m} \angle 3 \quad$ Prove: $\mathrm{m} \angle \mathrm{JOL}=\mathrm{m} \angle \mathrm{KOM}$

|  | Statement | Reason |
| :--- | :--- | :--- |
| 1. | $\mathrm{~m} \angle 1=\mathrm{m} \angle 3$ | Given |
| 2. | $\mathrm{~m} \angle 1+\mathrm{m} \angle 2=\mathrm{m} \angle 3+\mathrm{m} \angle 2$ | Addition Property of Equality |
| 3. | $\mathrm{~m} \angle 1+\mathrm{m} \angle 2=\angle \mathrm{JOL}$ | Angle Addition Property |
| 4. | $\mathrm{~m} \angle 2+\mathrm{m} \angle 3=\mathrm{m} \angle \mathrm{KOM}$ | Angle Addition Property |
| 5. | $\mathrm{~m} \angle \mathrm{JOL}=\mathrm{m} \angle \mathrm{KOM}$ | Substitution |
|  |  |  |
| 4.5 | $\mathrm{~m} \angle 2+\mathrm{m} \angle 3=\mathrm{m} \angle 3+\mathrm{m} \angle 2$ | Commutative Property |


6. Given: $\mathrm{m} \angle 1=90^{\circ} \quad$ Prove: $\mathrm{m} \angle 2+90^{\circ}=180^{\circ}$

|  | Statement | Reason |
| :---: | :--- | :--- |
| 1. | $\mathrm{m} \angle 1=90^{\circ}$ | Given |
| 2. | $\angle 1$ and $\angle 2$ are a linear pair | Definition of Linear Pair |
| 3. | $\angle 1$ and $\angle 2$ are supplementary | Linear Pair Theorem |
| 4. | $\mathrm{m} \angle 2+\mathrm{m} \angle 1=180^{\circ}$ | Definition of Supplementary |
| 5. | $\mathrm{m} \angle 2+90^{\circ}=180^{\circ}$ | Substitution |

7. Given: $\mathrm{PR} \cong \mathrm{LN}$

Prove: $P Q=L M$
$Q$ is midpoint of $P R$
$M$ is midpoint of LN

|  | Statement | Reason |
| :--- | :--- | :--- |
| 1. | $\mathrm{PR} \cong \mathrm{LN}$ | Given |
| 2. | $\mathrm{PR}=\mathrm{LN}$ | Definition of Congruence |
| 3. | Q is midpoint of PR; M is midpoint of LN | Given |
| 4. | $\mathrm{PQ} \cong \mathrm{QR} ; \mathrm{PQ}=\mathrm{QR}$ | Definitions of Midpoint \& Congruence |
| 5. | $\mathrm{LM} \cong \mathrm{MN;} \mathrm{LM} \mathrm{=} \mathrm{MN}$ | Definitions of Midpoint \& Congruence |
| 6. | $\mathrm{PR}=\mathrm{PQ}+\mathrm{QR} ; \mathrm{LN}=\mathrm{LM}+\mathrm{MN}$ | Segment Addition Postulate |
| 7. | $\mathrm{PQ}+\mathrm{QR}=\mathrm{LM}+\mathrm{MN}$ | Substitution |
| 8. | $\mathrm{PQ}+\mathrm{PQ}=\mathrm{LM}+\mathrm{LM}$ | Substitution |
| 9. | $2 \mathrm{PQ}=2 \mathrm{LM}$ | Combining Like Terms |
| 10. | $\mathrm{PQ}=\mathrm{LM}$ | Division Property of Equality |

8. Given: $\mathrm{EF} \perp \mathrm{EG}$

Prove: $\angle \mathrm{FED}$ and $\angle \mathrm{DEG}$ are complementary
D is in the interior of $\angle$ FEG

|  | Statement | Reason |
| :--- | :--- | :--- |
| 1. | EF $\perp$ EG | Given |
| 2. | $\mathrm{~m} \angle \mathrm{FEG}=90^{\circ}$ | Definition of Perpendicular |
| 3. | $\mathrm{~m} \angle \mathrm{FED}+\mathrm{m} \angle \mathrm{DEG}=\mathrm{m} \angle$ FEG | Angle Addition Postulate |
| 4. | $\mathrm{~m} \angle \mathrm{FED}+\mathrm{m} \angle \mathrm{DEG}=90^{\circ}$ | Substitution |
| 5. | $\angle$ FED and $\angle \mathrm{DEG}$ are complementary | Definition of Complementary |

9. Given: $A B \cong C D$

Prove: $A C \cong B D$

|  | Statement | Reason |
| :--- | :--- | :--- |
| 1. | $\mathrm{AB} \cong \mathrm{CD}$ | Given |
| 2. | $\mathrm{AB}=\mathrm{CD}$ | Definition of Congruence |
| 3. | $\mathrm{AB}+\mathrm{BC}=\mathrm{CD}+\mathrm{BC}$ | Addition Postulate of Equality |
| $4 \cdot$ | $\mathrm{AB}+\mathrm{BC}=\mathrm{AC}$ | Segment Addition Postulate |
| $5 \cdot$ | $\mathrm{BC}+\mathrm{CD}=\mathrm{BD}$ | Segment Addition Postulate |
| 6. | $\mathrm{AC}=\mathrm{BD}$ | Substitution |
| $7 \cdot$ | $\mathrm{AB} \cong \mathrm{CD}$ | Definition of Congruence |


10. Given: $\angle 1$ and $\angle 2$ are supplementary

Prove: $\angle 1$ and $\angle 2$ are right angles
$\angle 1 \cong \angle 2$

|  | Statement | Reason |
| :--- | :--- | :--- |
| 1. | $\angle 1$ and $\angle 2$ are supplementary | Given |
| 2. | $\mathrm{~m} \angle 1+\mathrm{m} \angle 2=180^{\circ}$ | Definition of Supplementary |
| 3. | $\angle 1 \cong \angle 2$ | Given |
| 4. | $\mathrm{~m} \angle 1=\mathrm{m} \angle 2$ | Definition of Congruent |
| 5. | $\mathrm{m} \angle 1+\mathrm{m} \angle 1=180^{\circ}$ <br> $\mathrm{m} \angle 2+\mathrm{m} \angle 2=180^{\circ}$ | Substitution |
| 6. | $2 \mathrm{~m} \angle 1=180^{\circ}$ <br> $2 \mathrm{~m} \angle 2=180^{\circ}$ | Combining Like Terms |
| 7. | $\mathrm{m} \angle 1=90^{\circ}$ <br> $\mathrm{m} \angle 2=90^{\circ}$ | Division Property of Equality |
| 8. | $\angle 1$ and $\angle 2$ are right angles | Definition of Right Angles |



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11. Given: $\angle 1 \cong \angle 2$

Prove: $\angle 1$ and $\angle 2$ are right angles

|  | Statement | Reason |
| :---: | :--- | :--- |
| 1. | $\angle 1 \cong \angle 2$ | Given |
| 2. | $\mathrm{~m} \angle 1=\mathrm{m} \angle 2$ | Definition of Congruent |
| 3. | $\angle 1$ and $\angle 2$ are a linear pair | Definition of Linear Pair |
| 4. | $\angle 1$ and $\angle 2$ are supplementary | Linear Pair Theorem |
| 5. | $\mathrm{m} \angle 1+\mathrm{m} \angle 2=180^{\circ}$ | Definition of Supplementary |
| 6. | $\mathrm{m} \angle 1+\mathrm{m} \angle 1=180^{\circ}$ <br> $\mathrm{m} \angle 2+\mathrm{m} \angle 2=180^{\circ}$ | Substitution |
| 7. | $2 \mathrm{~m} \angle 1=180^{\circ}$ <br> $2 \mathrm{~m} \angle 2=180^{\circ}$ | Combining Like Terms |
| 8. | $\mathrm{m} \angle 1=90^{\circ}$ <br> $\mathrm{m} \angle 2=90^{\circ}$ | Division Property of Equality |
| 9. | $\angle 1 \mathrm{and} \angle 2$ are right angles | Definition of Right Angles |


12. Given: $\angle 1$ and $\angle 2$ are complementary

Prove: $\angle 2$ and $\angle 3$ are complementary

|  | Statement | Reason |
| :--- | :--- | :--- |
| 1. | $\angle 1$ and $\angle 2$ are complementary | Given |
| 2. | $\mathrm{~m} \angle 1+\mathrm{m} \angle 2=90^{\circ}$ | Definition of Complementary |
| 3. | $\angle 1$ and $\angle 3$ are vertical angles | Definition of Vertical Angles |
| 4. | $\angle 1$ and $\angle 3$ are congruent | Vertical Angles Theorem |
| 5. | $\mathrm{~m} \angle 1=\mathrm{m} \angle 3$ | Definition of Congruent |
| 6. | $\mathrm{~m} \angle 3+\mathrm{m} \angle 2=90^{\circ}$ | Substitution |
| 7. | $\angle 2$ and $\angle 3$ are complementary | Definition of Complementary |


13. Given: $m \angle 2=2 m \angle 1$

Prove: $m \angle 1=60^{\circ}$

|  | Statement | Reason |
| :--- | :--- | :--- |
| 1. | $\mathrm{~m} \angle 2=2 \mathrm{~m} \angle 1$ | Given |
| 2. | $\angle 1$ and $\angle 2$ are a linear pair | Definition of Linear Pair |
| 3. | $\angle 1$ and $\angle 2$ are supplementary | Linear Pair Theorem |
| 4. | $\mathrm{~m} \angle 1+\mathrm{m} \angle 2=180^{\circ}$ | Definition of Supplementary |
| 5. | $\mathrm{~m} \angle 1+2 \mathrm{~m} \angle 1=180^{\circ}$ | Substitution |
| 6. | $3 \mathrm{~m} \angle 1=180^{\circ}$ | Combining Like Terms |
| 7. | $\mathrm{~m} \angle 1=60^{\circ}$ | Division Property of Equality |


14. Given: $A D$ bisects $\angle B A C$

Prove: $\angle 2 \cong \angle 3$

$$
\angle 1 \cong \angle 3
$$

|  | Statement | Reason |
| :--- | :--- | :--- |
| 1. | AD bisects $\angle \mathrm{BAC}$ | Given |
| 2. | $\angle 1 \cong \angle 2$ | Definition of Bisect |
| 3. | $\angle 1 \cong \angle 3$ | Given |
| 4. | $\angle 2 \cong \angle 3$ | Substitution |


15. Given: $\angle \mathrm{ABC}$ a right angle Prove: $\angle 1$ and $\angle 2$ are complementary

|  | Statement | Reason |
| :---: | :--- | :--- |
| 1. | $\angle A B C$ a right angle | Given |
| 2. | $\mathrm{~m} \angle \mathrm{ABC}=90^{\circ}$ | Definition of Right Angle |
| 3. | $\mathrm{~m} \angle 1+\mathrm{m} \angle 2=\mathrm{m} \angle \mathrm{ABC}$ | Angle Addition Postulate |
| 4. | $\mathrm{~m} \angle 1+\mathrm{m} \angle 2=90^{\circ}$ | Substitution |
| 5. | $\angle 1$ and $\angle 2$ are complementary | Definition of Complementary |



|  | Statement | Reason |
| :--- | :--- | :--- |
| 1. | $C D \cong E F$ | Given |
| 2. | $C D \cong F G$ | Given |
| 3. | EF $\cong F G$ | Substitution |
| 4. | F is midpoint of E | Definition of Midpoint |

17. Given: $K U \cong H F$

Prove: KH $\cong$ UF


|  | Statement | Reason |
| :--- | :--- | :--- |
| 1. | KU $\cong ~ H F ~$ | Given |
| 2. | $\mathrm{KU}=\mathrm{HD}$ | Definition of congruent |
| $3 \cdot$ | $\mathrm{KH}+\mathrm{HU}=\mathrm{KU}$ | Segment addition postulate |
| 4. | $\mathrm{HU}+\mathrm{UF}=\mathrm{HF}$ | Segment addition postulate |
| 5. | $\mathrm{KH}+\mathrm{HU}=\mathrm{HU}+\mathrm{UF}$ | Substitution |
| 6. | $\mathrm{KH}=\mathrm{UF}$ | Subtraction Prop of Equality |
| 7. | $\mathrm{KH} \cong \mathrm{UF}$ | Definition of congruent |

18. Given: $\angle \mathrm{ABD}$ and $\angle \mathrm{CDB}$ are right angles Prove: $\mathrm{m} \angle 1=\mathrm{m} \angle 3$
$\mathrm{m} \angle 2=\mathrm{m} \angle 4$

|  | Statement | Reason |
| :--- | :--- | :--- |
| 1. | $\angle \mathrm{ABD}$ and $\angle \mathrm{CDB}$ are right angles | Given |
| 2. | $\mathrm{~m} \angle \mathrm{ABD}=90^{\circ} ; \mathrm{m} \angle \mathrm{CDB}=90^{\circ}$ | Definition of right angles |
| 3. | $\mathrm{m} \angle \mathrm{ABD}=\mathrm{m} \angle \mathrm{CDB}$ | Substitution |
| 4. | $\mathrm{m} \angle 2=\mathrm{m} \angle 4$ | Given |
| 5. | $\mathrm{~m} \angle 1+\mathrm{m} \angle 2=\mathrm{m} \angle \mathrm{ADB}$ |  |
| $\mathrm{m} \angle 3+\mathrm{m} \angle 4=\mathrm{m} \angle \mathrm{CDB}$ |  |  |$\quad$ Angle Addition Postulate.


19. Given: $m \angle A B C=m \angle C B D$

Prove: $B C$ is the bisector of $\angle A B D$

|  | Statement | Reason |
| :--- | :--- | :--- |
| 1. | $\mathrm{m} \angle \mathrm{ABC}=\mathrm{m} \angle \mathrm{CBD}$ | Given |
| 2. | $\mathrm{~m} \angle \mathrm{ABC}+\mathrm{m} \angle \mathrm{CBD}=\mathrm{m} \angle \mathrm{ABD}$ | Angle Addition Postulate |
| 3. | $\mathrm{~m} \angle \mathrm{ABC} \cong \mathrm{m} \angle \mathrm{CBD}$ | Definition of congruent |
| 4. | BC is bisector of $\angle \mathrm{ABD}$ | Definition of bisector |


20. Given: $\mathrm{m} \angle \mathrm{ABE}=\mathrm{m} \angle \mathrm{CBE} \quad$ Prove: $\angle \mathrm{ABD}$ and $\angle \mathrm{DBE}$ are complementary

| Statement | Reason |
| :--- | :--- |
| 1. $\mathrm{m} \angle \mathrm{ABE}=\mathrm{m} \angle \mathrm{CBE}$ | 1. Given |
| 2. $\angle \mathrm{ABE} \cong \angle \mathrm{CBE}$ | 2. Def of congruent |
| 3. $\angle \mathrm{ABE}$ and $\angle \mathrm{CBE}$ are a linear pair | 3. Def of Linear Pair |
| 4. " "are supplementary | 4. Linear Pair Theorem |
| 5. $\mathrm{m} \angle \mathrm{ABE}+\mathrm{m} \angle \mathrm{CBE}=180^{\circ}$ | 5. Def of Supp |
| 6. $\mathrm{m} \angle \mathrm{ABE}+\mathrm{m} \angle \mathrm{ABE}=180^{\circ}$ | 6. Substitution |
| 7. $2(\mathrm{~m} \angle \mathrm{ABE})=180^{\circ}$ | 7. Simplify/Combine Like Terms |
| 8. $\mathrm{m} \angle \mathrm{ABE}=90^{\circ}$ | 8. Division Prop of E |
| 9. $\mathrm{m} \angle \mathrm{ABD}+\mathrm{m} \angle \mathrm{DBE}=\mathrm{m} \angle \mathrm{ABE}$ | 9. Angle Addition Prop |
| 10. $\mathrm{m} \angle \mathrm{ABD}+\mathrm{m} \angle \mathrm{DBE}=90^{\circ}$ | 10. Substitution |
| 11. $\angle \mathrm{ABD}$ and $\angle \mathrm{DBE}$ are complementary | 11. Def of Comp |



