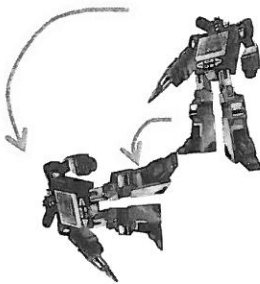
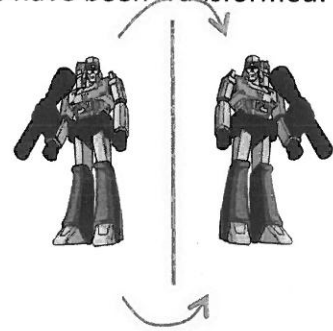
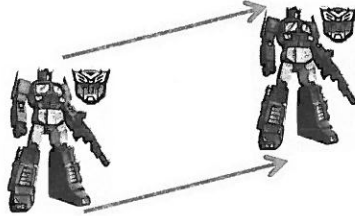


Write your questions here!

# Transformations

A transformation is when an image is changed in some way. The change could be a change in size, shape, or position. The following images have been transformed:



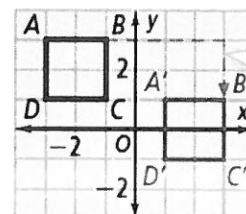
Translations, Reflections and Rotations are called \_\_\_\_\_ because the image is congruent to the \_\_\_\_\_.

# Translations

Take note

## Key Concept Translation

The diagram at the right shows a translation in the coordinate plane. Each point of the black square moves 4 units right and 2 units down. Using variables, you can say that each  $(x, y)$  pair in the original figure is mapped to  $(x', y')$ , where  $x' = x + 4$  and  $y' = y - 2$ . You can use arrow notation to write the following *translation rule*.



B moves 4 units right and 2 units down.

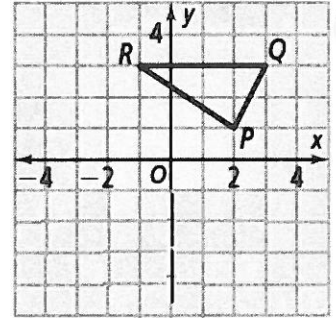
## 2 PACKET 8.1: TRANSLATIONS

Write your questions here!

### Example 1:

#### Finding the Image of a Translation

What are the images of the vertices of  $\triangle PQR$  for the translation  $(x, y) \rightarrow (x - 2, y - 5)$ ? Graph the image of  $\triangle PQR$ .



Identify the coordinates of each vertex. Use the translation rule to find the coordinates of each vertex of the image.

$$(x, y) \rightarrow (x - 2, y - 5)$$

$$P(2, 1) \rightarrow$$

$$Q(3, 3) \rightarrow$$

$$R(-1, 3) \rightarrow$$

To graph the image of  $\triangle PQR$ , first graph  $P'$ ,  $Q'$ , and  $R'$ . Then draw  $\overline{P'Q'}$ ,  $\overline{Q'R'}$ , and  $\overline{R'P'}$ .

What does the rule tell you about the direction each point moves?

$x' = x - 2$  means that each point moves 2 units left.  $y' = y - 5$  means that each point moves 5 units down.

There are three ways to write a translation:

\_\_\_\_\_ or \_\_\_\_\_ or \_\_\_\_\_

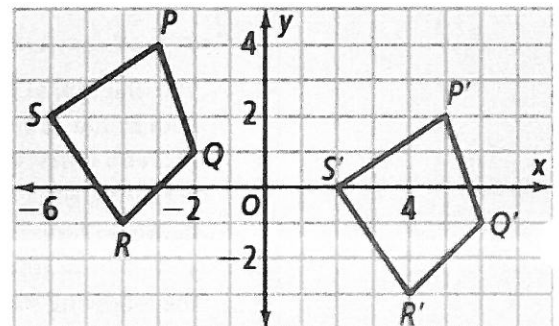
For example, a translation that moves a point 4 units right and 3 units down can be written as follows:

$P(x, y) \rightarrow$  \_\_\_\_\_ or \_\_\_\_\_ or \_\_\_\_\_  
 (Algebraic Rule) (Shorthand) (Vector notation)

### Example 2:

#### Writing a Rule to Describe a Translation

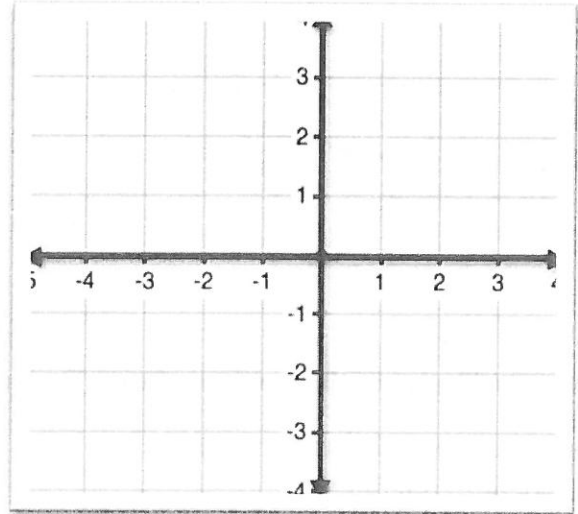
What is a rule that describes the translation  $PQRS \rightarrow P'Q'R'S'$ ?



Write your questions here!

**Example 3:**

Graph the image of the figure  $C(1, -2)$ ,  $A(-2, 1)$   $T(-3, -3)$  using the rule 1 unit left and 2 units up. Then, write the translation rule.

**Example 4:**

Write an algebraic rule to describe the transformation:

$$\begin{array}{c} C(2, 1), O(0, 0) L(-5, 4), D(-2, 1) \\ \text{to} \\ C'(0, 1), O'(-2, 0) L'(-7, 4), D'(-4, 1) \end{array}$$

**Example 5:**

Write an algebraic rule to describe the transformation:

$$\begin{array}{c} F(5, -2), R(10, 0) E(-5, 12), D(0, -3) \\ \text{to} \\ F'(23, -16), R'(28, -14) E'(13, -2), D'(18, -17) \end{array}$$

Now, summarize  
your notes here!

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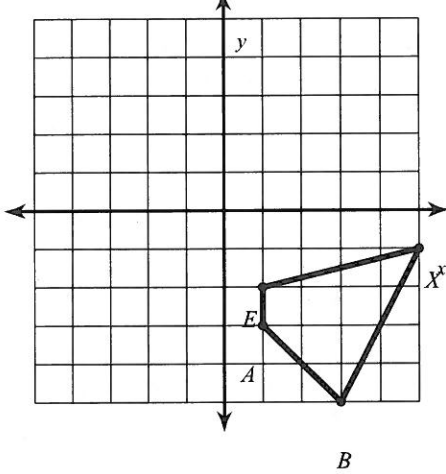
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Bist du bereit die Beherrschung-Check meistern? (Translate that!)

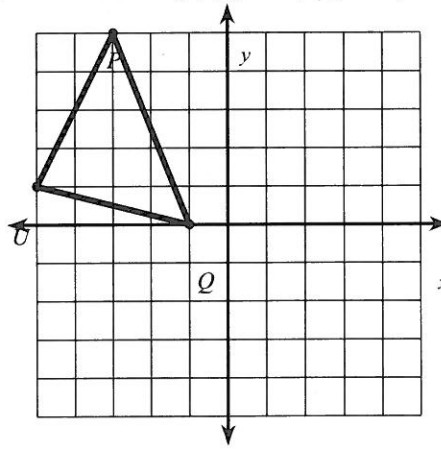
## EgVXi ^XZ' - #&

**Graph and label the image of the figure using the transformation given.**

1) translation:  $(x, y) \rightarrow (x - 4, y + 3)$



2) translation:  $(x, y) \rightarrow (x, y - 2)$



**Find the coordinates of the vertices of each figure after the given transformation.**

3) translation: 2 units left and 3 units up  
 $A(4, -5), S(3, -2), E(5, -5)$

4) translation: 1 unit left and 1 unit up  
 $D(-4, 0), J(0, 3), H(-1, -1)$

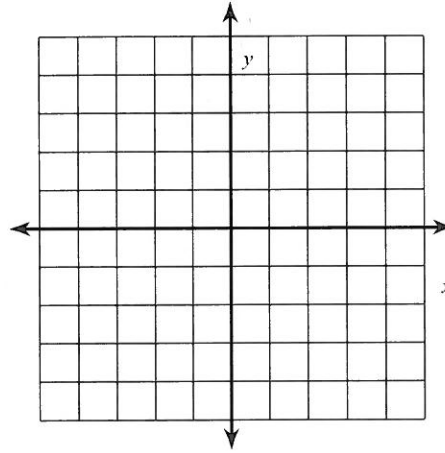
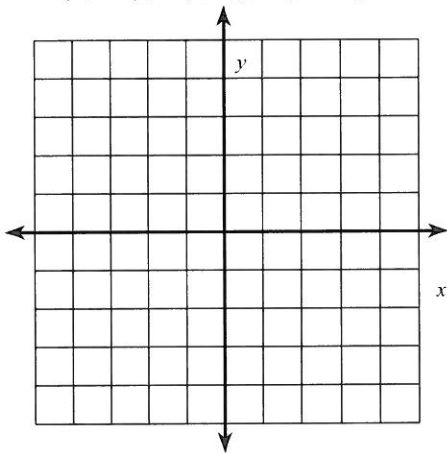
5) translation: 3 units up  
 $U(4, -3), P(3, 1), S(5, 1)$

6) translation: 1 unit right and 2 units down  
 $C(-1, -3), W(2, -2), N(4, -3)$

**Graph the image and the preimage of the figure using the transformation given.**

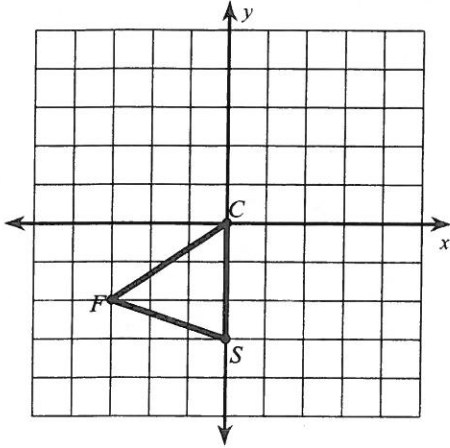
7) translation:  $(x, y) \rightarrow (x - 5, y + 4)$   
 $C(2, -3), V(3, 1), R(5, -2)$

8) translation:  $(x, y) \rightarrow (x - 1, y + 4)$   
 $R(-3, -3), D(0, 1), C(1, 0)$

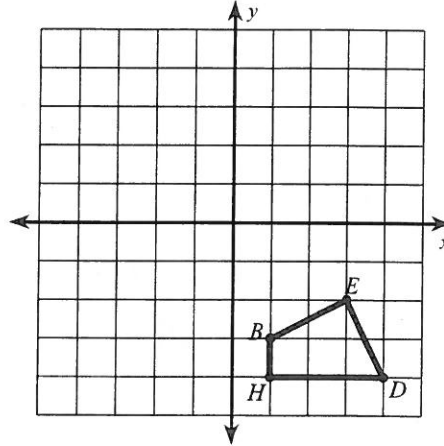


Graph the image of the figure using the transformation given.

9) translation:  $(x, y) \rightarrow (x + 3, y)$

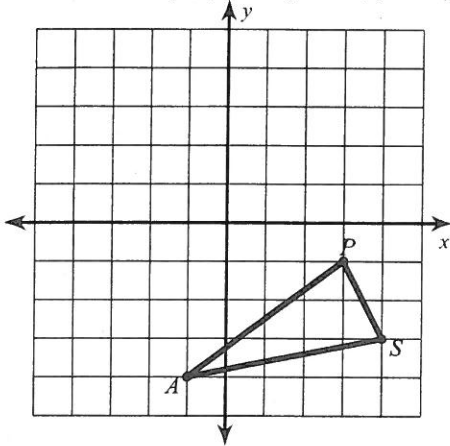


10) translation:  $(x, y) \rightarrow (x - 1, y + 5)$

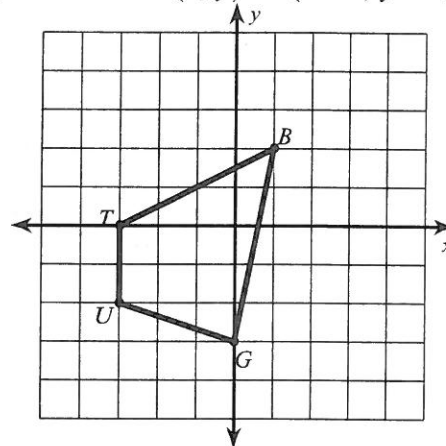


Find the coordinates of the vertices of each figure after the given transformation.

11) translation:  $(x, y) \rightarrow (x - 3, y - 1)$



12) translation:  $(x, y) \rightarrow (x + 3, y - 2)$

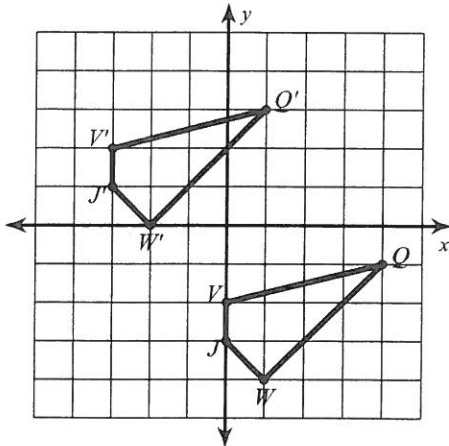


13) translation:  $(x, y) \rightarrow (x - 5, y + 4)$   
 $H(1, -1), W(2, 0), E(4, -5), Y(3, -5)$

14) translation:  $(x, y) \rightarrow (x + 6, y - 3)$   
 $M(-4, 4), Z(-4, 5), E(-1, 5), K(-1, 3)$

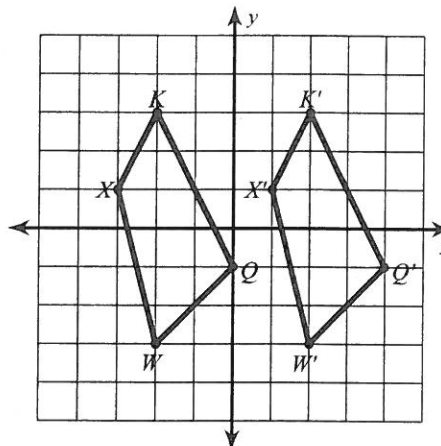
Write an algebraic rule to describe each transformation.

15)



1)  $L(-5, -3), X(-4, -1), J(-3, -1), Z(-5, -5)$   
 to  
 $L'(-2, -2), X'(-1, 0), J'(0, 0), Z'(-2, -4)$

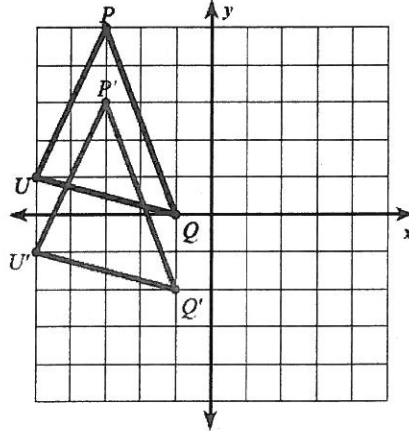
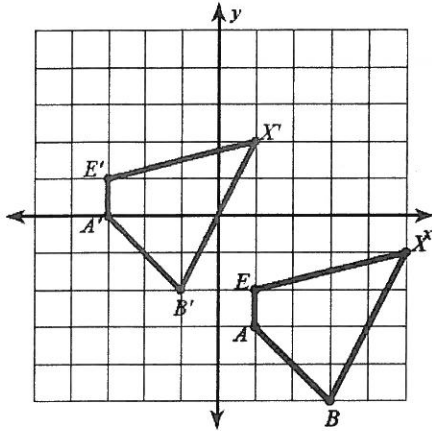
16)



18)  $V(-1, -3), T(-3, 0), B(-3, 1), R(1, -2)$   
 to  
 $V'(2, -2), T'(0, 1), B'(0, 2), R'(4, -1)$

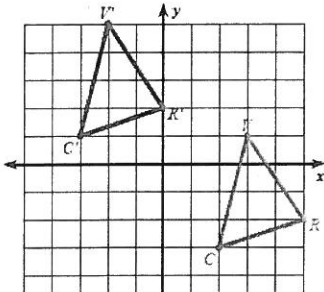
## Practice 8.1 Answers

- 1) translation:  $(x, y) \rightarrow (x - 4, y + 3)$     2) translation:  $(x, y) \rightarrow (x, y - 2)$

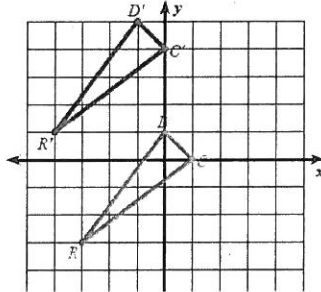


3.  $A'(2, -2), S'(1, 1), E'(3, -2)$   
 4.  $D'(-5, 1), J'(-1, 4), H'(-2, 0)$   
 5.  $U'(4, 0), P'(3, 4), S'(5, 4)$   
 6.  $C'(0, -5), W'(3, -4), N'(5, -5)$

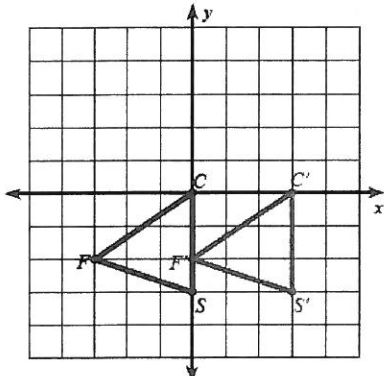
- 7) translation:  $(x, y) \rightarrow (x - 5, y + 4)$   
 $C(2, -3), V(3, 1), R(5, -2)$



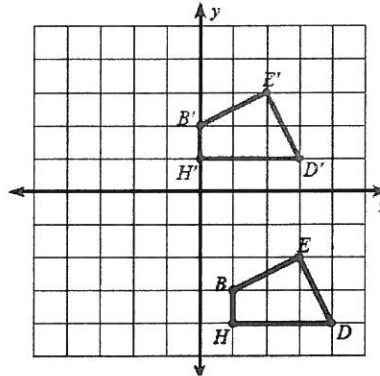
- 8) translation:  $(x, y) \rightarrow (x - 1, y + 4)$   
 $R(-3, -3), D(0, 1), C(1, 0)$



- 9) translation:  $(x, y) \rightarrow (x + 3, y)$



- 10) translation:  $(x, y) \rightarrow (x - 1, y + 5)$



11.  $A'(-4, -5), P'(0, -2), S'(1, -4)$   
 12.  $U'(0, -4), T'(0, -2), B'(4, 0), G'(3, -5)$   
 13.  $H'(-4, 3), W'(-3, 4), E'(-1, -1), Y'(-2, -1)$   
 14.  $M'(2, 1), Z'(2, 2), E'(5, 2), K'(5, 0)$   
 15. translation:  $(x, y) \rightarrow (x - 3, y + 4)$   
 17. translation:  $(x, y) \rightarrow (x + 3, y + 1)$

16. translation:  $(x, y) \rightarrow (x + 4, y)$   
 18. translation:  $(x, y) \rightarrow (x + 3, y + 1)$