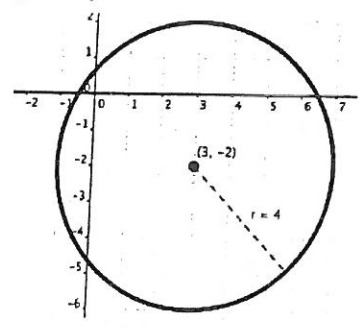


Name: Answer key
 Serafino • Precalculus S1

Per: 3/7 Date: 12/14/15

3D Circles in Radians
 Notes / Classwork



EQUATION OF A CIRCLE: $(x - h)^2 + (y - k)^2 = r^2$ where (h, k) is center
 $(x - 3)^2 + (y + 2)^2 = 16$

1. Find the requested information. Sketch if necessary.

a. Center: (5, -2) Radius: 6

Equation: $(x - 5)^2 + (y + 2)^2 = 36$

Domain: $x \in [-1, 11]$

Range: $y \in [-8, 4]$

b. Center (-4, 0) Diameter 10 $r = 5$

Equation: $(x + 4)^2 + y^2 = 25$

Domain: $x \in [-9, 1]$

Range: $y \in [-5, 5]$

c. Center (0, 3): Radius: $\sqrt{14}$

Equation: $x^2 + (y - 3)^2 = 14$

Domain: $x \in [-\sqrt{14}, \sqrt{14}]$

Range: $y \in [3 - \sqrt{14}, 3 + \sqrt{14}]$

d. Center at the origin, Diameter: ~~6~~ $6\sqrt{2}$ $r = 3\sqrt{2}$

Equation: $x^2 + y^2 = 18$

Domain: $x \in [-3\sqrt{2}, 3\sqrt{2}]$

Range: $y \in [-3\sqrt{2}, 3\sqrt{2}]$

2. Write the equations of the circle:

a. Center (3, 7) Point on circle: (6, 11) $r = \sqrt{4^2 + 3^2} = 5$

$(x - 3)^2 + (y - 7)^2 = 25$

c. Center (-2, 5), Point on circle: (-3, 7) $r = \sqrt{2^2 + 1^2} = \sqrt{5}$

$(x + 2)^2 + (y - 5)^2 = 5$

b. Center is the origin, Point: (-2, -6) $\sqrt{6^2 + 2^2} = \sqrt{36 + 4} = \sqrt{40}$

$x^2 + y^2 = 40$

3. Determine if a point is on the circle: Think about the relationship between x, y and the radius. $x^2 + y^2 = r^2$

a. Are the following points on the Unit Circle? If no, state if it is in or outside.

$(\frac{\sqrt{5}}{3}, \frac{\sqrt{2}}{3})$ No, inside
 $(\frac{-\sqrt{7}}{5}, \frac{\sqrt{32}}{5})$ No, outside
 $(\frac{-\sqrt{2}}{2}, \frac{-\sqrt{2}}{2})$ yes, on

$(\frac{\sqrt{5}}{3})^2 + (\frac{\sqrt{2}}{3})^2 \stackrel{?}{=} 1$
 $\frac{7}{25} + \frac{32}{25} \stackrel{?}{=} 1$
 $\frac{2}{4} + \frac{2}{4} = 1$

$\frac{7}{9} < 1$

b. A circle has the equation: $(x-2)^2 + (y-3)^2 = 8$. Are the following points in, on, or outside the circle?

$(-1, 3)$ $(4, 5)$ $(0, 1)$ $(2, 5)$

$(-1-2)^2 + (3-3)^2 \stackrel{?}{=} 8$
 $(4-2)^2 + (5-3)^2 = 8$
 $(-2)^2 + (1-3)^2 = 8$
 $0^2 + 2^2 = 8$

$(3)^2 + 0^2 \stackrel{?}{=} 8$
 $2^2 + 2^2 = 8$
 $2^2 + 2^2 = 8$

$9 > 8$ outside
 $4 + 4 = 8$ on
on
inside

4. Name the coordinates of the point (x, y) intersected by the terminal side of an angle, θ , in standard position. If the angle is special, give an exact value as well as an approximation. $(x, y) = (r \cos \theta, r \sin \theta)$

a. $r=3, \theta = \pi/3$
 c. $r=5, \theta = 5\pi/4$
 e. $r=6, \theta = 5\pi/3$ $(6 \cdot \frac{1}{2}, 6 \cdot -\frac{\sqrt{3}}{2})$

$= (\frac{3}{2}, \frac{3\sqrt{3}}{2})$
 $= (-\frac{5\sqrt{2}}{2}, -\frac{5\sqrt{2}}{2})$
 $= (3, -3\sqrt{3})$

$\approx (1.5, 2.5981)$
 $\approx (-3.536, -3.536)$
 $\approx (3, -5.1962)$

b. $r=4, \theta = 7\pi/30$
 d. $r=20, \theta = 199\pi/180$
 f. $r=10, \theta = 5\pi/9$

$(2.9726, 2.6765)$
 $(-18.9104, -6.5114)$
 $(-1.7365, 9.8481)$

5. Approximate a solution for θ , where $0 \leq \theta < 2\pi$ for a circle with a center at the origin:

a. $r=3$, Point $(2.8978, 0.7765)$
 b. $r=6$ Point $(\frac{3\sqrt{3}}{6}, \frac{1}{2}, \frac{\sqrt{3}}{2})$
 c. $r=\sqrt{2}$ Point: $(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}})$

$3 \cos \theta = 2.8978$
 $\cos \theta = 0.9659$
 $\theta \approx 0.2618$

$\theta = \frac{\pi}{3}$
 $\theta = \frac{\pi}{4} \approx 0.7854$

≈ 1.047

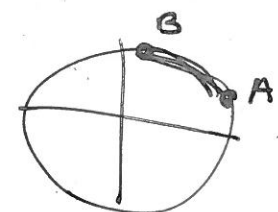
6. Find the length of the arc between the points on a circle with a center at the origin:

a. $r=5$, A $(4.5315, 2.1131)$ B $(0.4358, 4.981)$

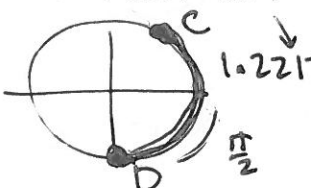
$\theta = 0.43635$
 $\theta = 1.4835$

$S = 5.23587$ units

$\widehat{AB} \theta = 1.04717$



b. $r=7$, C $(2.3941, 6.5778)$ D $(0, -7)$



$\theta = 1.2217$

$\theta = 1.2217 + \frac{\pi}{2}$

$= 2.7925$

$S = 19.5477$ units