Name: $\qquad$ Per: $\qquad$ Date: $\qquad$
Serafino • Precalculus S2

## 7R Matrices Unit Review

You may want to do work on a separate piece of paper.

Matrix Operations:

$$
A=\left[\begin{array}{ccc}
1 & 2 & 3 \\
4 & 5 & 6
\end{array}\right] \quad B=\left[\begin{array}{ccc}
-2 & 3 & 1 \\
4 & -5 & 0
\end{array}\right] \quad D=\left[\begin{array}{ll}
1 & 4 \\
2 & 3
\end{array}\right] \quad\left[\begin{array}{cc}
2 & 0 \\
4 & -1 \\
6 & 3
\end{array}\right]
$$

1. Perform the operations without a calculator:
a. $3 A-2 B$
b. $\quad C^{3}$
c. $\quad 2 A-\left(B+D^{\top}\right)$
d. DB
e. $\mathrm{C}^{-1}$
f. $|B D|-|C|$
g. Solve for Matrix X:
$B-2 X=A$
2. Perform the operation with a calculator:

$$
E=\left[\begin{array}{ccc}
2 & -1 & 3 \\
0 & 4 & 1 \\
-6 & -2 & 4
\end{array}\right]
$$

a. $|E|$
b. $\mathrm{E}^{-1}$
3. Find the area of Triangles: a) Set up the Matrix Determinant formula b) Calculate the area with a calculator
a

b.

c.


Solving Systems with Cramer's Rule: a) Set up the system b) Set up the Cramer's Rule b) Do the math with a calc.
4. On the quiz, you will only be asked to use Cramer's rule to solve for ONE variable. So, for the problems below, you're going to a) pick a variable to solve for b) SET UP Cramer's rule for that variable c) Use your calc to solve. $\star$ Some systems may need some rearranging...
a. $\quad-5 x-5 y=25$
$-2 x-4 y=16$
b. $\quad x-3 y=5$
$-3 x+6 y=8$
c. $\quad-4 x-6 z=-12$
$-6 x-4 y-2 z=6$
$-x+2 y+z=9$
d. $\quad-6 x-y+z=-7$

$$
\begin{aligned}
& 4 z=-6 \\
& 4 x-24 y+24 z=17
\end{aligned}
$$

e. $\quad 3 a+b=-c+7$
$a+3 b-c=13$
$b=2 a-1$
f. $\quad 13=3 x-y$
$14 y-3 x+2 z=-3$
$z=2 x-4 y$

## Applications of Matrix Multiplication \& Solving with RREF:

5. The School Play: The play is running for three nights: Opening night (Thursday), the Second night (Friday) and the Final night (Saturday). People placed online orders for tickets in the following quantities, which can be represented in the Sales table to the right:

| Performance | Adults | Students |
| :--- | :---: | :---: |
| Opening night | 420 | 300 |
| Second night | 400 | 450 |
| Final night | 510 | 475 |

a) Write the Sales Matrix S . Write another Sales Matrix, $\mathrm{S}^{\top} \quad$ (Label rows/columns to help you)
b) What cell in matrix $S$ represents the least number of students going?

Why could that be?
c) What cell in matrix $S$ represents the least number of adults going?

Why could that be?
d) Student tickets are $\$ 5$ and adult tickets are $\$ 10$, write a matrix, $C$, that represents the cost of each type of ticket. Note: You could write FOUR different types of matrices.

Does the order of adults vs. students matter?
e) Multiply two matrices to find how much money was taken in each night.

What is the total revenue?
f) Ugh! The theater department wants to be able to buy an Audrey II for Little Shop of Horrors next year, and to do so, it actually need $\$ 20,000$ total revenue from the play. They decide to keep it open for a $4^{\text {th }}$ night, at a far cheaper price so they can make it to their goal. Adult tickets will still be twice as much as student tickets. The sales for the $4^{\text {th }}$ night are exactly like the second night. Set up and solve a matrix equation that shows how much should the theater department charge for each type of ticket to hit their target revenue?
6. Ba-da-bababa:

I'm buying McDonalds for all my Precalc classes. These are their orders:
a) Turn the table into Matrix O , the Order Matrix. Also, write $\mathrm{O}^{\top}$.

|  | Page 3 of 4 |  |  |
| :---: | :---: | :---: | :---: |
| Orders: | Per 1 | Per 3 | Per 5 |
| Big Macs | 6 | 8 | 4 |
| Wraps | 5 | 3 | 10 |
| Salads | 2 | 6 | 4 |
| McNuggets | 2 | 4 | 3 |
| Fries | 2 | 3 | 2 |

b) I look it up online, and see: A 20-pc Nuggets box is $\$ 5$, Salad is $\$ 4.79$, Big Mac is $\$ 3.99$, a Wrap is $\$ 1.69$ and a large Fries is $\$ 1.79$. Pick one of your Matrix Os and write Matrix P, a Price matrix, so that when you multiply them, you can see how much this lunch going to cost me, per class period. Label rows and columns to make life easy.
c) Matrix C (right) represents how many TOTAL calories each class consumed by eating Big Macs, McNuggets and Salads. Define your variables and set up a linear system and use RREF to solve for how many calories, each item.

|  | Total Calories |
| :---: | :---: |
| Per 1 | 5,302 |
| Per 3 | 9,316 |
| Per 5 | 5.908 |

d) How many calories are in each individual nugget?

Setting up and Solving Systems with RREF:
For each of the situations below, a) define your variables, b) Set up linear equations, c) Solve.
7. San Diego Diner: Ron \& Veronica ordered breakfast at a diner. Ron paid $\$ 3.25$ for 4 eggs and 2 pancakes. Veronica paid $\$ 3.50$ for 2 eggs and 2 pancakes. What is the cost of each item?
8. Taping Shows: You make a VHS tape of your three favorite TV shows for your friend: Family Guy, Lost, and One Tree Hill. You can completely fill the tape with 7 episodes. You want include twice as many episodes of Lost as Family Guy. An episode of Family Guy lasts 30 minutes. An episode of Lost and One Tree Hills lasts 60 minutes. Your VCR tape can only hold 360 minutes of recording. How many episodes of each show can you tape?
9. Arcade: The local arcade uses 3 different colored tokens for their game machines. For $\$ 20$, you can buy the following options of token packages: 14 gold, 20 silver and 24 bronze OR 20 gold, 15 silver and 19 bronze OR 30 gold, 5 silver, 13 bronze. How much is each token worth?

## Setting up and Solving for ONE VARIABLE with CRAMER'S RULE:

10. Track Meet: RHS competed in a track meet. They had 20 students won medals in first, second or third place in various events. First place is worth 5 points, second place is worth 3 points, and third place is worth 1 point. The students at RHS won total of 68 points. The number of second place finishes was as many as first and third place combined. How many runners finished in FIRST place?
11. Dogs \& Cats: You want to make some money over the summer and you have a completely empty house, so you decide to watch pets when the families in your neighborhood when they're away. You can accommodate 68 animals in your home. You know you can handle 3 times as many cats as dogs. You want to keep things clean, so you'll need 4 more litter boxes than the number of cats. How many LITTER BOXES do you need
