

Name: Answer Key  
 Serafino • Algebra 2E

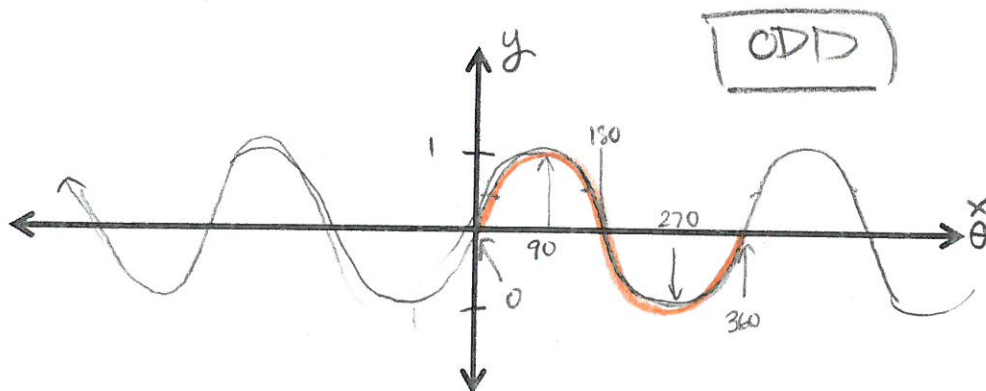
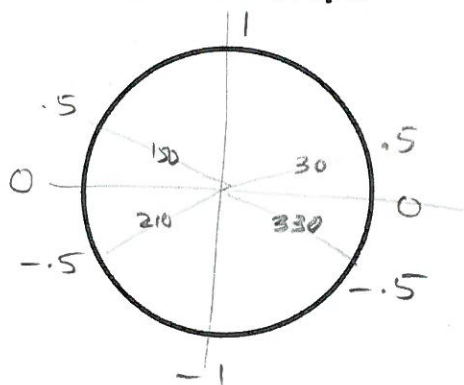
Per: \_\_\_\_\_ Date: \_\_\_\_\_

## 9B1 Graphing Sinusoids – Packet 1 (AD)

SA = Sinusoidal Axis  
 A = Amplitude  
 NP = Natural Period  
 B = Frequency  
 P = Period  
 I = Increment

The horizontal “average” of the function. Also called a “midline”  
 How many units above/below the function goes (from the SA or midline)  
 The “natural period” of the parent function; how long it takes to complete one cycle  
 How many cycles the trig function completes in its natural period  
 The period of THIS function; how long to repeat the cycle?  $P = NP / B$   
 The critical values of input (hits average, max or min)  $I = P/4$ .

### The Sine Graph



Domain:  $x \in \mathbb{R}$

Natural Period  $360^\circ$

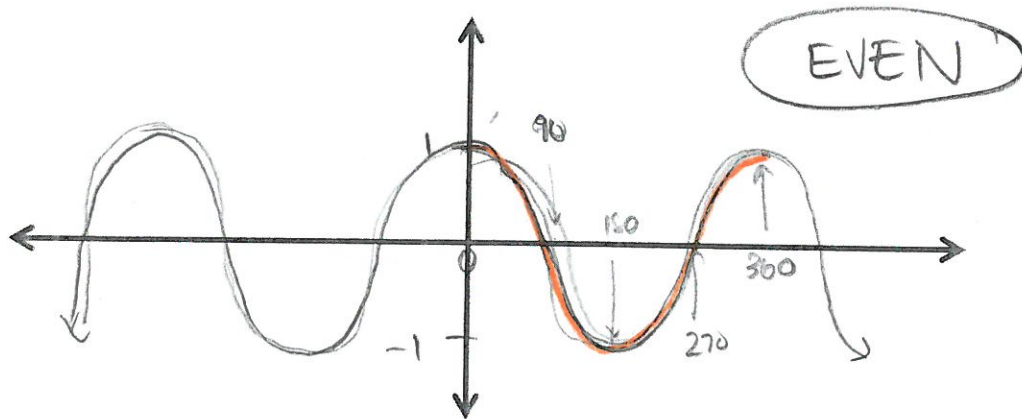
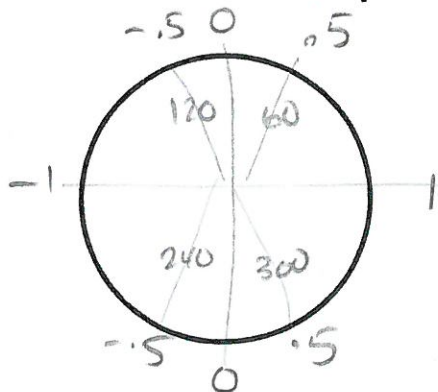
Amplitude: 1

Range:  $y \in [-1, 1]$

Increment:  
 $\frac{P}{4} = \frac{360}{4} = 90^\circ$

Sinusoidal Axis:  $y = 0$

### The Cosine Graph



Domain:  
 $x \in \mathbb{R}$

Natural Period  $360^\circ$

Amplitude: 1

Range:  
 $y \in [-1, 1]$

Increment:  
 $\frac{P}{4} = \frac{360}{4} = 90^\circ$

Sinusoidal Axis:  $y = 0$

$$f(x) = A \sin (Bx \pm C) \pm D$$

Your mission:

Make sure your settings are in degrees, the domain is  $-700$  to  $700$ , and your range is  $-10$  to  $10$ .

Set up a parent function in the first spot:  $(\sin x$  or  $\cos x)$

Set up a second function in second spot, with different numbers.

✱  $f(x) = A \sin (x)$

Enter: First function:  $y = \sin x$   
 Second function:  $y = 2 \sin x$

What affect(s) does A have on the graph?

Vertical stretch/compress  
 - Reflect over x-axis

Play with second function:  $3 \sin x$ ,  $5 \sin x$ ,  $\frac{1}{2} \sin x$ ,  $\frac{1}{3} \sin x$ , ...

See what happens when you make A negative.  $3 \sin x$ ,  $5 \sin x$ ,  $\frac{1}{2} \sin x$ ,  $-4 \sin x$ ,  $\frac{1}{3} \sin x$ .

$f(x) = \sin (Bx)$

Enter: First function:  $y = \sin x$   
 Second function:  $y = \sin 2x$

What affect does B have on the graph?

Horizontal stretch/compress

Play with second function:  $\sin 3x$ ,  $\sin 5x$ ,  $\sin \frac{1}{2} x$ ,  $\sin \frac{1}{3} x$ , .....

✱  $f(x) = \sin (x) \pm D$

Enter: First function:  $y = \sin (x)$   
 Second function:  $y = \sin (x) + 2$

What affect does D have on the graph?

shift up/down

Play with second function:  $\sin (x) + 3$ ,  $\sin (x) - 1$ ,  $\sin (x) - \frac{1}{2}$

$f(x) = \sin (x + c)$

Enter: First function:  $y = \sin (x)$   
 Second function:  $y = \sin (x + 30)$

What affect does C have on the graph?

shift left/right

Play with second function:  $\sin (x + 45)$ ,  $\sin (x - 90)$ ,  $\sin (x + 360)$ ,  $\sin (x - 20)$ , ...

**Recall Even/Odd Functions:**

As we graph these, keep in mind Even/Odd - ness.

EVEN:

Opposite input = same output

"opposite input"

PDD

Opposite input = opposite output

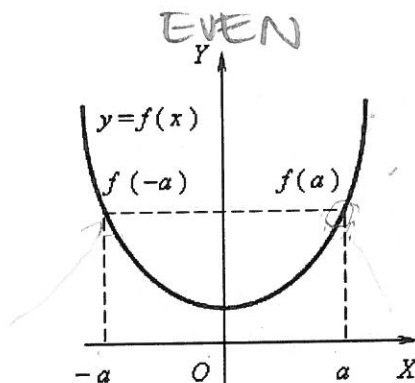


Fig 5

if  $f(x) = x^2 + 1$   
 $f(3) = 10$   
 $f(-3) = 10$

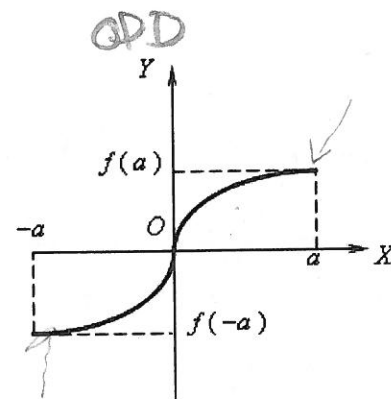
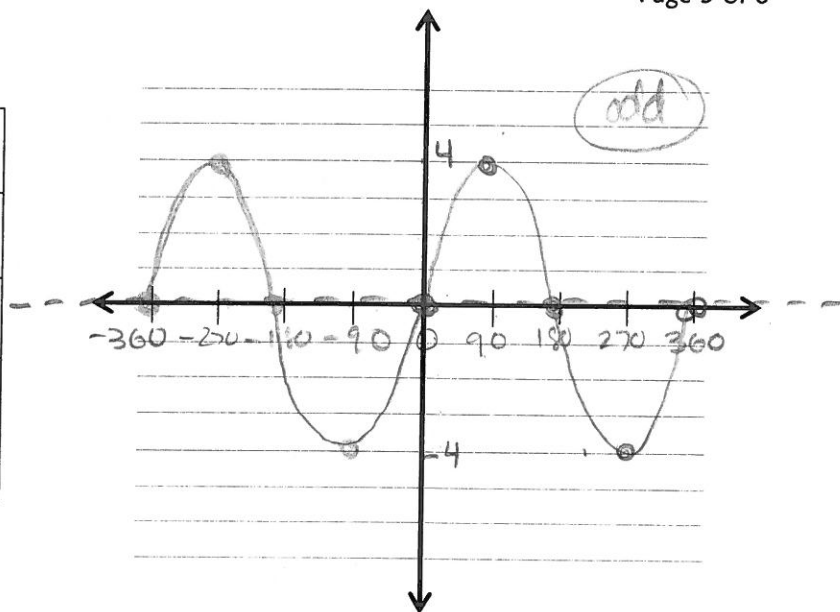


Fig 6

if  $f(x) = \sqrt[3]{x}$   
 $f(8) = 2$   
 $f(-8) = -2$

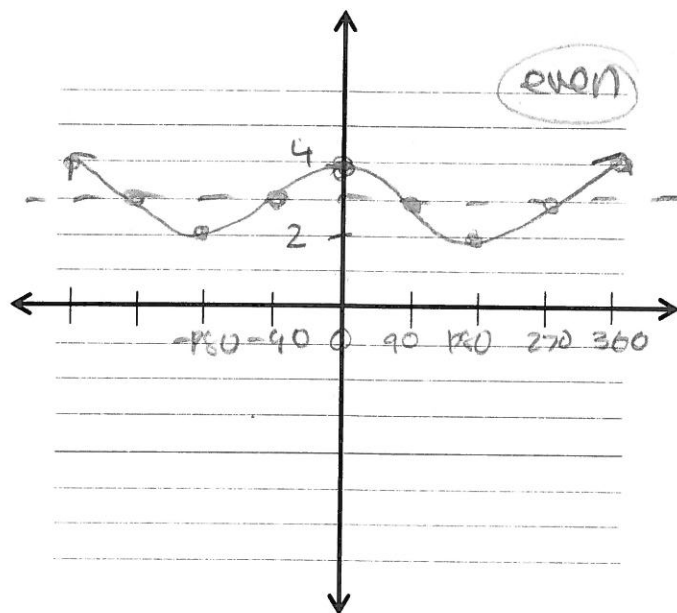
1.  $y = 4 \sin(x)$

A	4	SA	$y=0$
D	$x \in \mathbb{R}$		
R	$y \in [-4, 4]$		
P	$360^\circ$		
I	$P/4 = 360/4 = 90^\circ$		



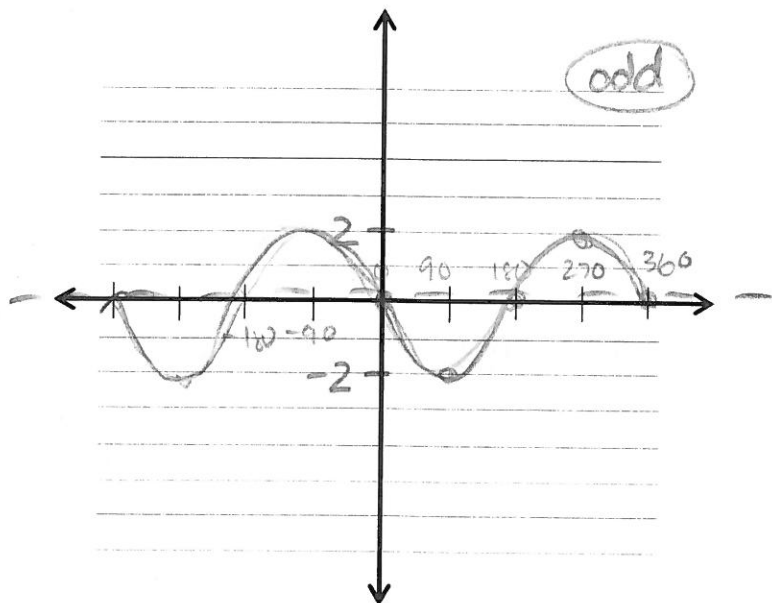
2.  $y = \cos(x) + 3$

A	1	SA	$y=3$
D	$x \in \mathbb{R}$		
R	$y \in [2, 4]$		
P	$360^\circ$		
I	$90^\circ$		



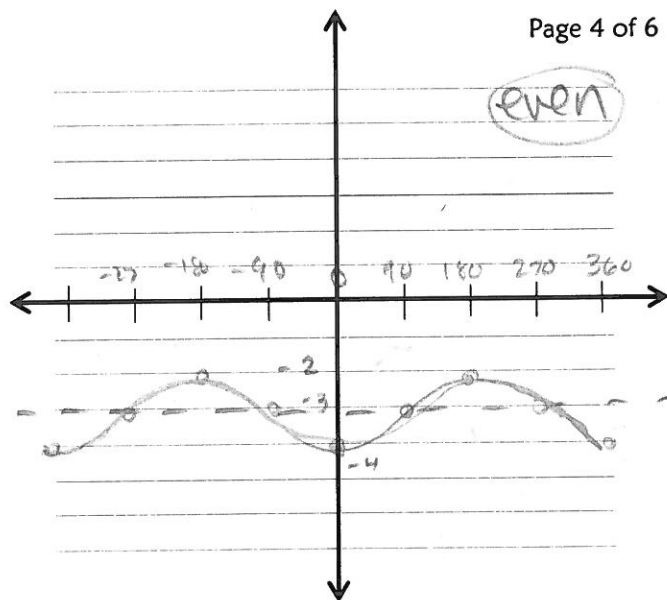
3.  $y = -2 \sin(x)$

A	2	SA	$y=0$
D	$x \in \mathbb{R}$		
R	$y \in [-2, 2]$		
P	$360^\circ$		
I	$90^\circ$		



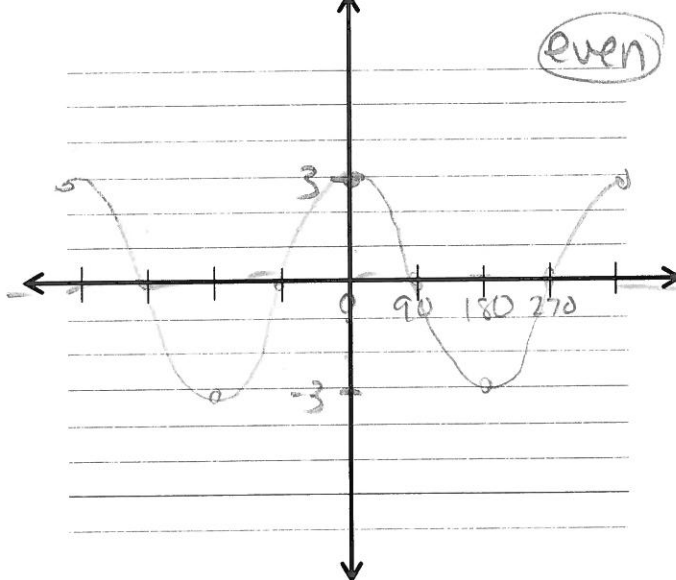
4.  $y = -\cos(x) - 3$

A	1	SA	$y = -3$
D	$x \in \mathbb{R}$		
R	$y \in [-4, -2]$		
P	$360^\circ$		
I	$90^\circ$		



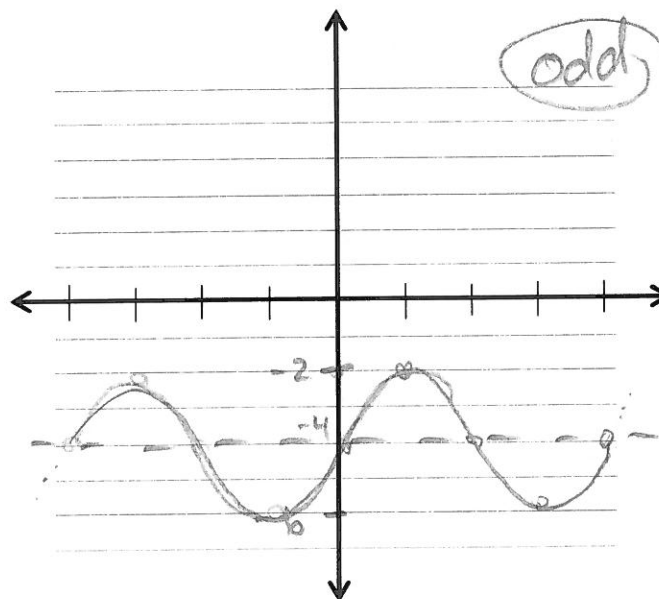
5.  $y = 3 \cos(x)$

A	3	SA	$y = 0$
D	$x \in \mathbb{R}$		
R	$y \in [-3, 3]$		
P	$360^\circ$		
I	$90^\circ$		



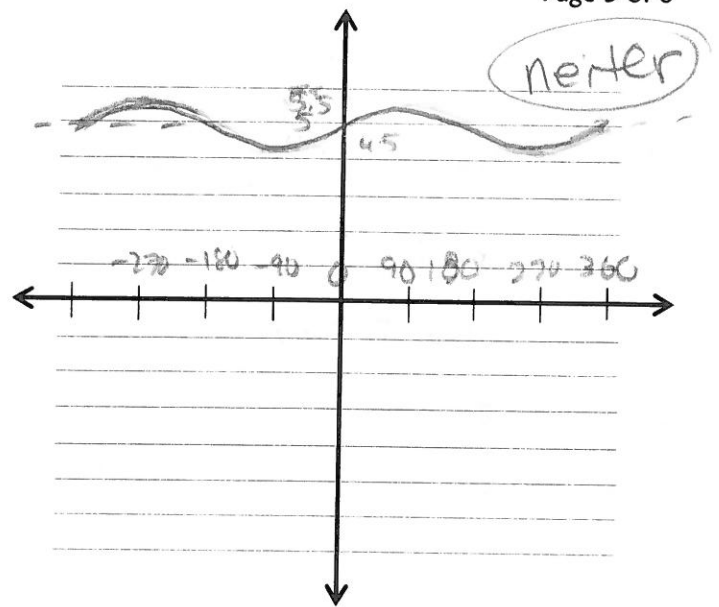
6.  $y = 2 \sin(x) - 4$

A	2	SA	$y = -4$
D	$x \in \mathbb{R}$		
R	$y \in [-6, -2]$		
P	$360^\circ$		
I	$90^\circ$		



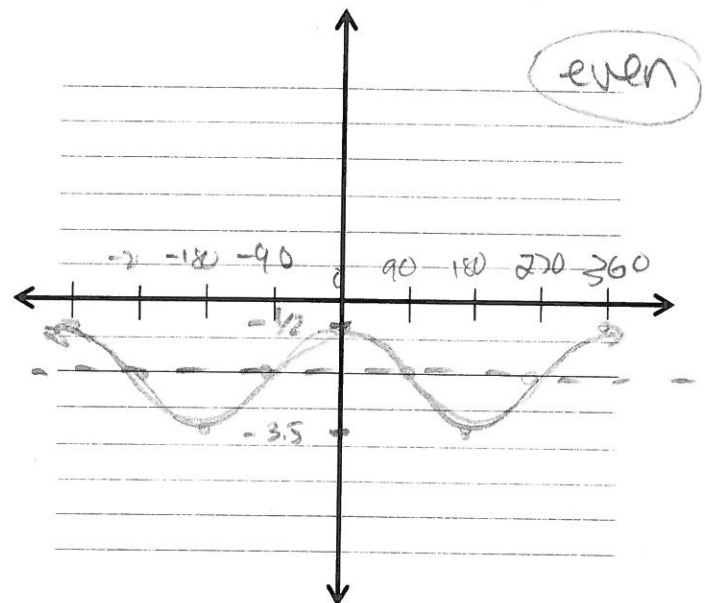
7.  $y = \frac{1}{2} \sin(x) + 5$

A	$\frac{1}{2}$	SA	$y = 5$
D	$x \in \mathbb{R}$		
R	$y \in [4.5, 5.5]$		
P	$360^\circ$		
I	$90^\circ$		



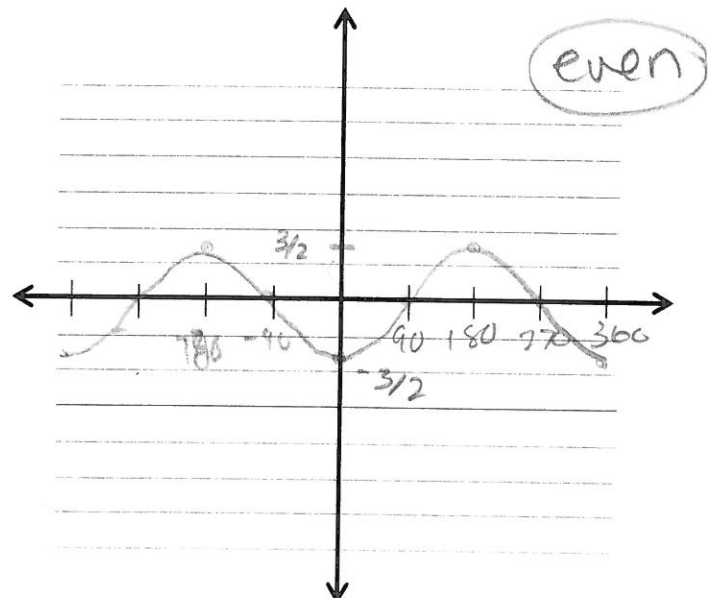
8.  $y = \frac{3}{2} \cos(x) - 2$

A	$\frac{3}{2}$	SA	$y = -2$
D	$x \in \mathbb{R}$		
R	$y \in [-3.5, -.5]$		
P	$360^\circ$		
I	$90^\circ$		



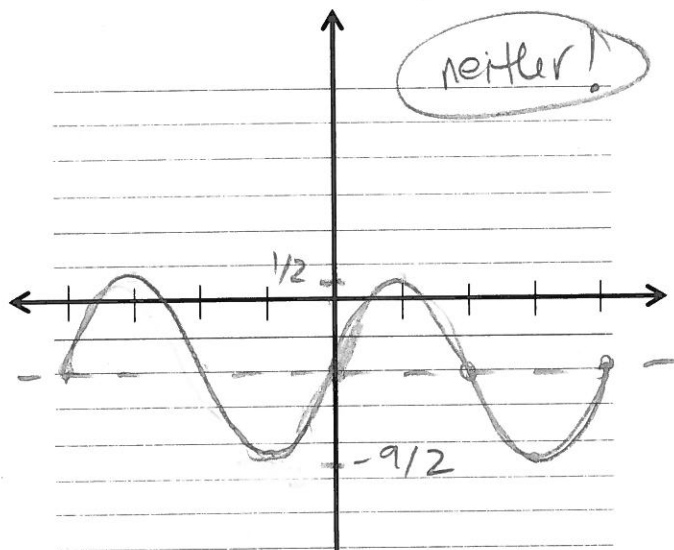
9.  $y = -\frac{3}{2} \cos(x)$

A	$\frac{3}{2}$	SA	$y = 0$
D	$x \in \mathbb{R}$		
R	$y \in [-\frac{3}{2}, \frac{3}{2}]$		
<del>B</del>			
P	$360^\circ$		
I	$90^\circ$		



10.  $y = \frac{7}{2} \sin(x) - 2$

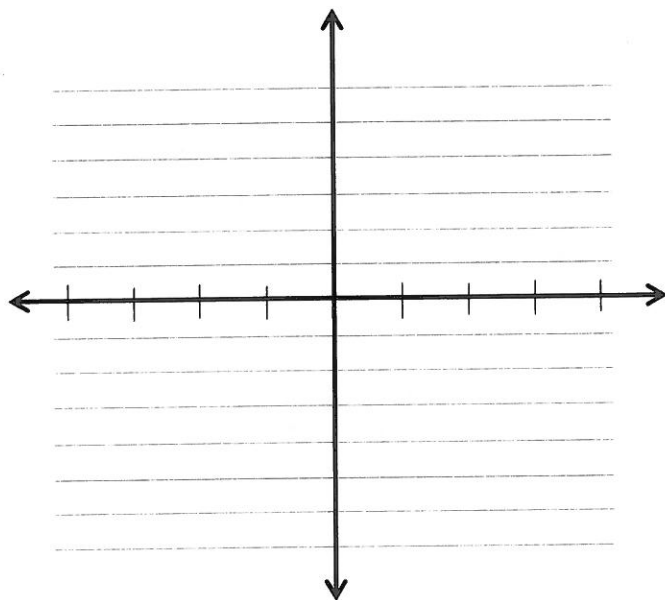
A	7/2	SA	$y = -2$
D	$x \in \mathbb{R}$		
R	$y \in [-9/2, 1/2]$		
P	$360^\circ$		
I	$90^\circ$		



\* In class!

11.  $y = 3 \sec(x)$

A		SA	
D			
R			
P			
I			



\* In class!

12.  $y = -\csc(x) + 2$

A		SA	
D			
R			
P			
I			

