

6D

Even / Odd Functions

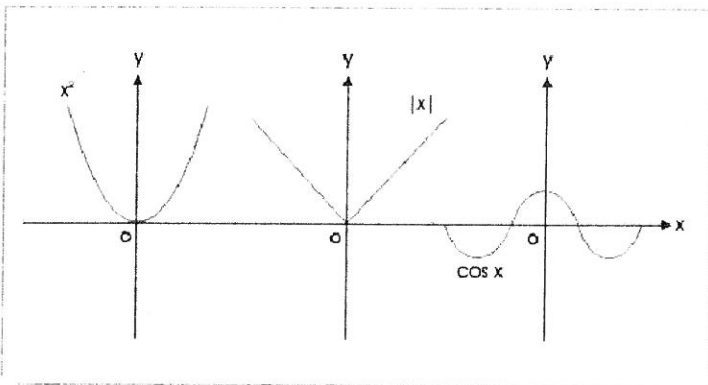
Class Activity

A new way to classify functions: In the world of functions, we can classify functions by degree (linear, quadratic, radical, etc) and number of terms (monomial, trinomial, etc). There are other classifications out there that can apply to ANY function or relation. Functions are either **EVEN, ODD or NEITHER**.

EVEN Functions

Visually: Y-axis is the axis of symmetry
 Reflection over the y-axis ($x = 0$)

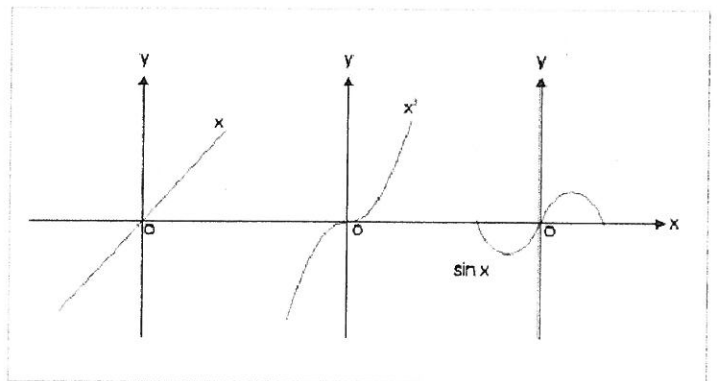
Algebraically: $f(-x) = f(x)$



ODD Functions

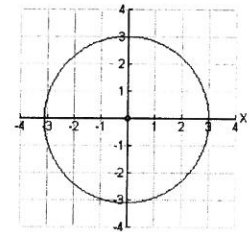
Visually: 180° rotational symmetry about the origin
 Double reflection over y-axis AND x-axis

Algebraically: $f(-x) = -f(x) = -f(-x)$



A FUNCTION can be even, odd, or neither. Most parent functions will be either even or odd. See above. A few parent functions are neither. We've done of those already.

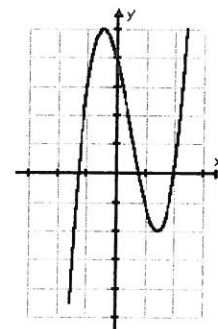
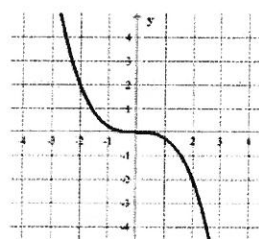
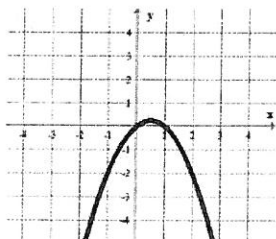
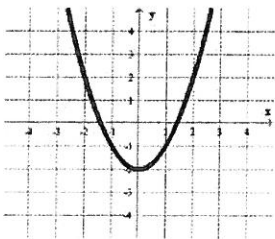
A RELATION (equations that are not functions) can be even, odd, neither or can be both. A good example of this is a circle: $x^2 + y^2 = 9 \rightarrow$



In your math travels, you will be asked to verify if a function is even or odd, or neither. You can do this visually, from a graph, or algebraically, from evaluation. Both are easy.

Determining Even/Oddness from a Graph:

Check for y-axis symmetry or if it's a 180° spin around the origin (double reflection)



A: _____

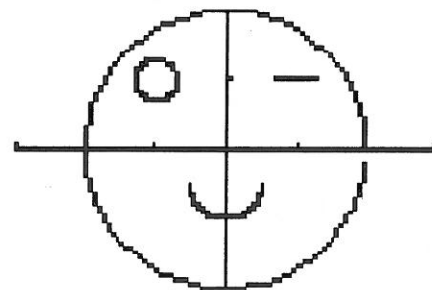
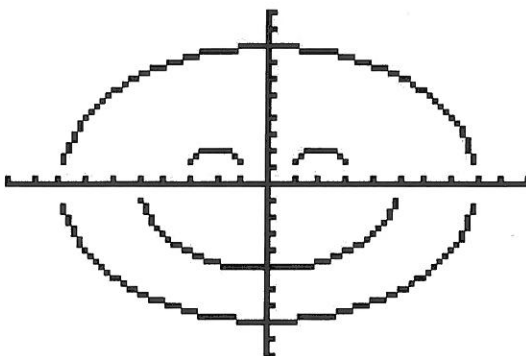
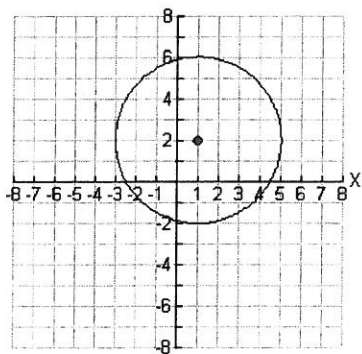
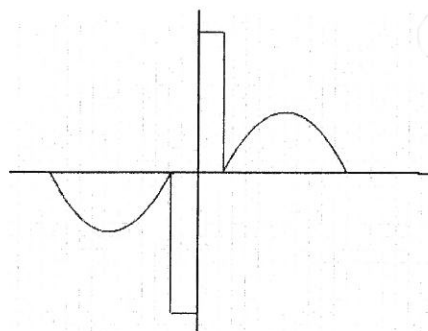
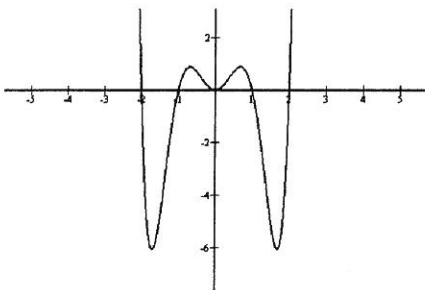
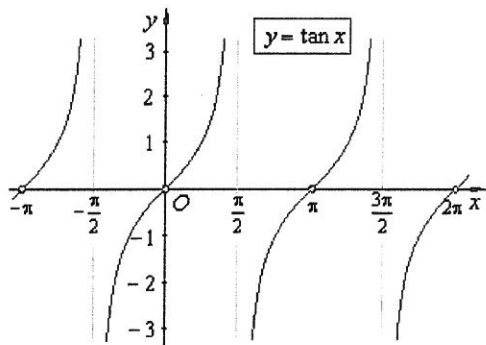
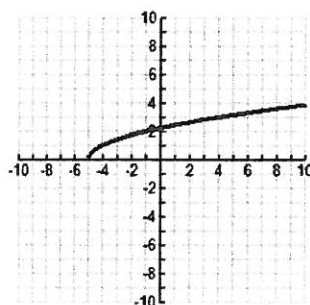
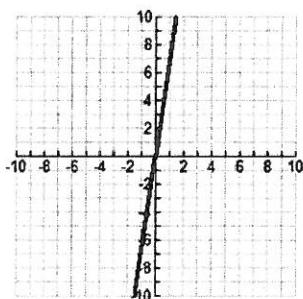
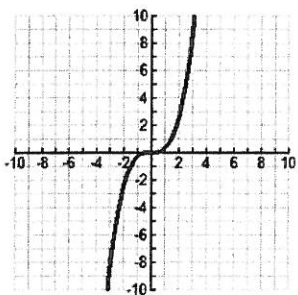
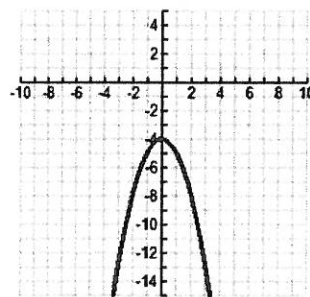
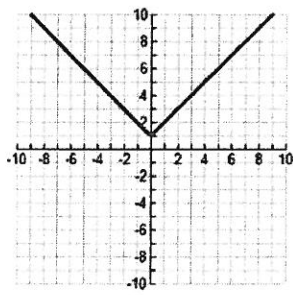
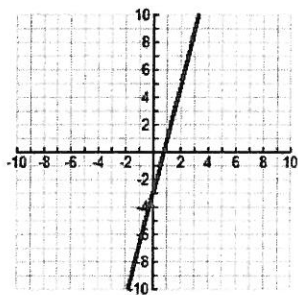
B: _____

C: _____

D: _____

Now you try!

1. Evenness/Oddness from a Graph: Determine if the following graphs are of functions that are even, odd, or neither.



Determining Evenness/Oddness from a function:

It's easy. Evaluate $f(x)$ at a number. Then evaluate $f(-x)$.

If it's the same, then it's even. If it's the opposite, then it's odd.

Ex 1: $y = 2x$

Test: $f(5) = 10$

Test $f(-5) = -10$

So it's odd!

Ex 2: $y = x^2 - 3$

Test: $f(5) = 22$

Test $f(-5) = 22$

So it's even!!

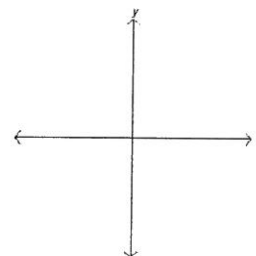
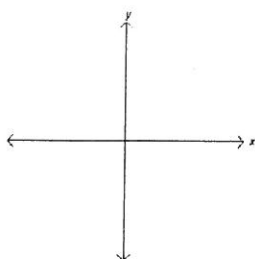
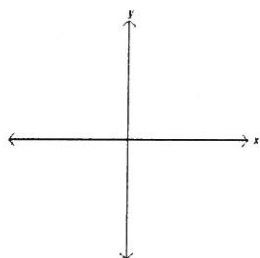
Ex 3: $y = |x - 5|$

Test $f(5) = 0$

Test $f(-5) = 10$

Neither!

You can also kind of "cheat" the system by simply knowing what these functions look like.



Now you try!

2. Determine, algebraically, if the following functions/relations are even, odd or neither:

$f(x) = 3x^2$

$f(x) = x^3 - 2$

$f(x) = 3x + 4$

$f(x) = x^2 - 5$

$f(x) = 10x + 5$

$f(x) = 2(x+1)^3$

$f(x) = \sin(x)$

$f(x) = \cos(x)$

$f(x) = 2|x| + 10$

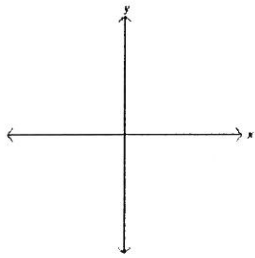
$f(x) = x^{1/2}$

$f(x) = 2x^3 + 3x$

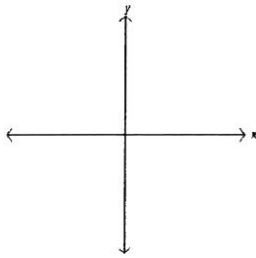
$f(x) = 1/x$

Practice: Determine if the function is even, odd, or neither. Sketch to confirm.

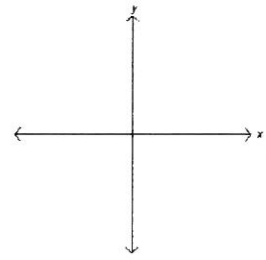
1. $y = -5x$



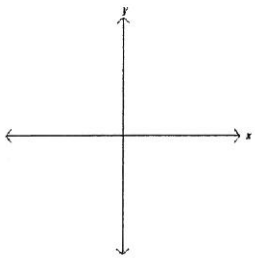
2. $y = |x| + 3$



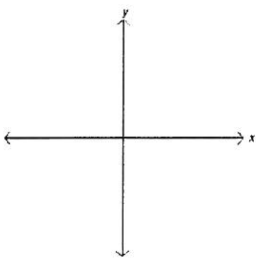
3. $y = \frac{1}{2}x - 3$



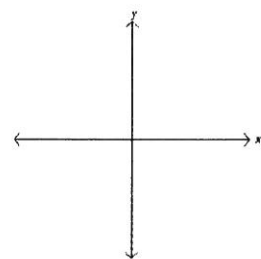
4. $y = x^2 + 1$



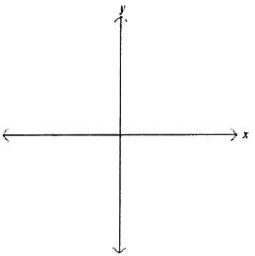
5. $y = \sqrt{x+2}$



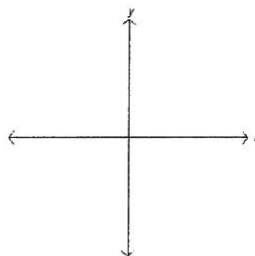
6. $y = -\sqrt[3]{x}$



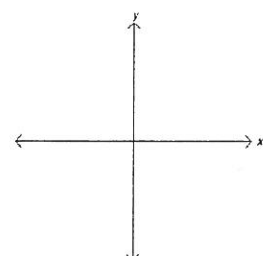
7. $y = \frac{4}{x}$



8. $y = x^4 - 4x^2$ aka $x^2(x+2)(x-2)$

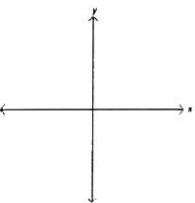


9. $y = \sqrt{x^3}$

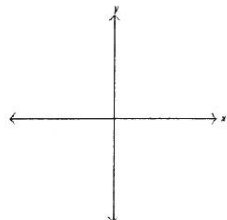


Use Desmos.com to graph these funky ones!

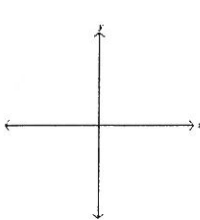
$y = \sqrt{x^2 - 1}$



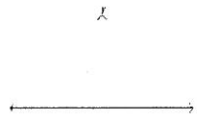
$y = \frac{x^2}{x^2 - 9}$



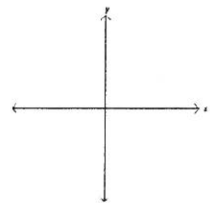
$y = -(x)^{\frac{2}{3}}$



$y = \sin x + \sin 3x$



$y = \sin 4x - x$



BONUS: A young grasshopper asked, "Is there a **function** that is both even and odd?". The sensei replied, "Yes, there is one, so it is shy. If you graph it lightly, you may not see it, as it hides behind what is already there."